A Compact, Passive Frequency-Hopping Harmonic Sensor Based on a Microfluidic Reconfigurable Dual-Band Antenna

Liang Zhu, Mohamed Farhat, Yi-Chao Chen, Khaled N Salama, Senior Member, IEEE, and Pai-Yen Chen, Senior Member, IEEE

Abstract—We propose here a fully-passive wireless liquid sensor using a harmonic transponder, which comprises a dual-band microstrip antenna reconfigured by different types of liquids injected in a fluidic cavity. Different from traditional radio-frequency (RF) backscatter sensors, the proposed harmonic-transponder sensor (or harmonic sensor) receives frequency-hopped RF monotones and backscatters their second harmonics, with the peak frequency shifted by dielectric properties of liquid mixtures. This microstrip antenna has a hybrid-feed structure, of which an outer split-ring patch exhibits a narrow-band TM_{102} mode at the fundamental frequency ($f_0$) and an inner elliptical patch displays a wideband resonance centered at the second-harmonic frequency (2$f_0$), achieved with hybridization of TM_{111} and TM_{110} modes. In particular, the outer split-ring patch is loaded with a fluidic channel system to tune the resonance frequency of the TM_{102} mode ($f_0$). We demonstrate that the type of liquid mixture filling in the fluidic cavity can be clearly perceived by reading the peak received signal strength indicator (RSSI) in the spectrum of second harmonics. Our results show the potential for deploying this passive wireless sensor in noisy environments that include clutters, multiple reflections, jamming, and crosstalks.

Index Terms—antenna sensors, harmonic-transponder sensors, passive wireless sensors, microstrip antennas, clutters, cross talks, electromagnetic interferences.

I. INTRODUCTION

Wireless sensing and tracking are core technologies that enable many applications in the scope of internet-of-things (IoT), industrial 4.0, wireless healthcare, and smart city, to name a few [1]-[4]. In most wireless sensing systems, a reader or interrogator transmits a continuous wave (CW) radio-frequency (RF) signal to power a tag and receives backscattered signals that are modulated by a sensor or actuator on the tag [5]-[7]. Along with development of ubiquitous massive sensors, the ever-increasing wireless nodes and the combination of heterogeneous networks have already generated a time-varying and rich-scattering complex environment filled with echoes, clutters, crosstalks and other electromagnetic interference sources. Very recently, the concept of harmonic sensor was inspired by the concept of harmonic radar, and has gained considerable attention because it provides a longer detection range and an enhanced signal-to-noise ratio (SNR) for electrically-small passive wireless sensors [8]-[12]. These harmonic sensors can be classified as nonlinear antenna sensors, whose resonant frequency can be sensitively reconfigured by the dielectric characteristics of the sample under test (SUT) [13]-[16]. Unlike traditional radio-frequency identification (RFID)-based passive sensors, a compact harmonic sensor receives and backscatters RF signals at orthogonal frequencies to avoid clutters and crosstalks. The types of liquids inside the microfluidic cavity can be known by analyzing the frequency hopping spread spectrum (FHSS) pattern.

Fig. 1. Schematics and sensing mechanism of a frequency-hopping harmonic sensor based on the proposed dual-band microstrip antenna. The antenna displays a liquid-reconfigured narrow resonance at the fundamental frequency ($f_0$) and an insensitive wideband resonance centering in the second-harmonic band (2$f_0$). The full-passive harmonic sensor receives and backscatters RF signals at orthogonal frequencies to avoid clutters and crosstalks. The types of liquids inside the microfluidic cavity can be known by analyzing the frequency hopping spread spectrum (FHSS) pattern.

L. Zhu and P. Y. Chen are with the Department of Electrical and Computer Engineering, University of Illinois, Chicago, IL 60607, USA.

Y. C. Chen is with the Department of Computer Science and Engineering, Shanghai Jiao Tong University, Shanghai 200240, China.

M. Farhat and K. N. Salama are with the Division of Computer, Electrical, and Mathematical Science and Engineering, King Abdullah University of Science and Technology (KAUST), Thuwal 23955-6900, Saudi Arabia.

This work was supported by NSF ECCS-CCSS under Grant 1914420. Corresponding author: P. Y. Chen; e-mail: pychen@uic.edu
until now, harmonic sensors still suffer from several pitfalls. For example, they generally require dual antennas, i.e., a $R_x$ antenna to receive the fundamental tone ($f_0$) and a $T_x$ antenna to retransmit the harmonic signal (e.g., second harmonic or $2f_0$) [28], [29], which inevitably increases the overall sensor/tag size and cost. Besides, wireless readout that relies merely on detecting the amplitude of backscattered second harmonic could still struggle with errors and data misinterpretation due to path loss and reflections of second harmonic. Although the wide-spectrum absolute resonance sensing could address this issue, microstrip antennas used in traditional RFID systems are usually narrowband [28], [29], and, therefore, not suitable for wide-spectrum applications.

In this paper, we propose a compact, reconfigurable dual-band microstrip antenna that can be used for making a low-profile passive harmonic sensor to monitor liquid density in real time. Specifically, this harmonic sensor adopts the robust wide-spectrum absolute resonance sensing [Fig. 1] that has not yet been explored in existing RFID sensor systems. This antenna excites a narrowband resonant mode at $f_0$ and a broadband resonance at $2f_0$, which is necessary for the frequency-hopping harmonics-based sensing. In addition, as understood from the eigenmodal analysis, the microstrip antenna is properly loaded with a fluidic cavity such that perturbations caused by the liquid’s dielectric properties can shift the resonance frequency $f_0$, while not affecting the broadband resonance around $2f_0$. Consequently, a nonlinear, wide-spectrum absolute resonance sensing scheme can be achieved by analyzing the frequency hopping spread spectrum (FHSS) of the reader, as illustrated in Fig. 1.

In the proposed wireless sensing system, the reader’s transceiver ($T_x$) transmits a constant-strength frequency-hopping sequence with 20 channels [$f_1$, $f_2$, …, $f_{20}$] to the harmonic sensor equipped with the proposed dual-band antenna. These hopping signals are received in sequence by the harmonic sensor, undergoing the frequency doubling process [$f_1$, $f_2$, …, $f_{20}$] → [2$f_1$, 2$f_2$, …, 2$f_{20}$], and being re-transmitted to the portable sniffer (e.g. smart phone with 5G and LTE antenna covering the frequency band of interest). The dielectric property of the SUT can effectively modulate the antenna’s resonance frequency $f_0$, which will be extracted by post-processing the high-dimensional FHSS pattern [2$f_1$, 2$f_2$, … 2$f_{20}$], as sketched in

Table I

<table>
<thead>
<tr>
<th>Dimension</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$L$</td>
<td>85</td>
</tr>
<tr>
<td>$L_1$</td>
<td>22</td>
</tr>
<tr>
<td>$W$</td>
<td>85</td>
</tr>
<tr>
<td>$W_1$</td>
<td>22</td>
</tr>
<tr>
<td>$h_1$</td>
<td>1.5</td>
</tr>
<tr>
<td>$h_2$</td>
<td>1.5</td>
</tr>
<tr>
<td>$h_3$</td>
<td>0.1</td>
</tr>
<tr>
<td>$a$</td>
<td>16.5</td>
</tr>
<tr>
<td>$b$</td>
<td>15.675</td>
</tr>
<tr>
<td>$d_1$</td>
<td>3.2</td>
</tr>
<tr>
<td>$d_2$</td>
<td>5</td>
</tr>
</tbody>
</table>

Fig. 2. Geometry and dimensions of the proposed dual band microstrip antenna with fluidic channel: (a) 3-D view. (b) Top view of the microstrip antenna. (c) Top view of the three-layers fluidic channel.

Fig. 3. Simulation results for snapshots of electric field $E_z$: (a) TM$_{310}$ mode at 1.31 GHz, (b) TM$_{410}$ mode at 2.55 GHz, and (c) TM$_{510}$ mode at 2.64 GHz.
The FHSS pattern analysis can provide robust and accurate absolute resonance sensing, which is not possible with one-dimensional data obtained from traditional non-hopping harmonic RFID sensors.

II. THEORETICAL MODELING OF DUAL-BAND PATCH ANTENNA

We have studied a compact, dual-resonance microstrip antenna composed of a concentric outer split-ring patch and an inner circular patch, which respectively resonate at $f_0$ (TM$_{310}$ mode of the split-ring patch antenna) and $2f_0$ (TM$_{110}$ mode of the circular patch antenna), provided that feed points are suitably located [30]. However, both resonant modes have a narrow bandwidth. In order to perform the FHSS analysis, the inner circular patch must be replaced by the geometry that gives a wideband resonance. An elliptical patch with tailorable even and odd resonant modes could be the simplest possible design for effectively increasing the bandwidth around $2f_0$. Additionally, unlike our previous work utilizing a rectangular patch with a microcavity to perturbate its TM$_{010}$ mode [31], we further integrate the dual-resonance microstrip antenna with a practical fluidic channel loaded with different sample-under-tests (SUTs). Fig. 2 shows the geometry of the proposed dual-band microstrip antenna consisting of an elliptical patch, a concentric split-ring patch, and a fluidic channel integrated on top. The proposed patch layer is separated from the ground plane by the FR4 substrate with relative permittivity $\varepsilon_r = 4.2$, thickness $h = 1.6$ mm, and loss tangent $\delta = 0.015$. Given the fact that the antenna has a negligible thickness compared to operating wavelengths, resonance frequencies can be predicted by the cavity model [32]-[34]. In our case, two open cavities with concentric split-ring and elliptical shapes are considered, respectively. The perfect electric conductor (PEC) boundary conditions are applied to top and bottom layers of these two cavities, and the perfect magnetic conductor (PMC) is assumed for their sidewalls. The transcendental equation for the split-ring resonant cavity can be derived as [30]:

$$J'_n(kR_c)Y''_n(kR_c) - J''_n(kR_c)Y'_n(kR_c) = 0,$$

$$n = \frac{m\pi}{2\pi - \theta_0} \text{ for } m = 1, 2, 3, \ldots, \tag{1}$$

where $J'_n(\cdot)$ and $Y''_n(\cdot)$ are the Bessel functions of the first and the second kinds, $k = \omega \sqrt{\varepsilon_r \mu_r R_c}$, and $\theta_0$ are the free-space permittivity and permeability. Based on Eq. (1), we have designed the split-ring patch antenna with $m = 3$ (TM$_{310}$ mode), $R_2 = 38.2$ mm, $R_3 = 22$ mm, and $\theta_0 = 30^\circ$, which provides a narrow-band resonance at the fundamental frequency (1.31 GHz here).

For the elliptical cavity with the reference elliptical coordinate $(\xi, \eta)$, where $\xi \in [0, a]$ and $\eta \in [0, b]$ \textsuperscript{\[35], [36]} \textsuperscript{\[35], [36]} \textsuperscript{\[35], [36]} \textsuperscript{\[35], [36]} \textsuperscript{\[35], [36]} \textsuperscript{\[35], [36]}, the transcendental equations can be reduced to the following set, with PMC boundary conditions assumed at the sidewall $\xi = \xi_0$:

$$M_{e,n}(\xi_0, q) = 0 \text{ for } n\text{-th even mode}$$

$$M_{o,n}(\xi_0, q) = 0 \text{ for } n\text{-th odd mode} \tag{2}$$

where $q = c'k^2 / 4$, the semi-focal length $c = \sqrt{a^2 - b^2}$, $M_{e,n}(\xi, q)$ and $M_{o,n}(\xi, q)$ are respectively the even and odd radial Mathieu function of the first kind, $n$ is the order of the angular Mathieu functions $C_{e,n}(\eta, q)$ and $S_{e,n}(\eta, q)$, which determine the azimuthal variation along $\eta$ [37], [38]. By solving the above transcendental equation with $\xi_0 = 1.83$ ($a = 16.5$ mm, and $b = 15.675$ mm), the first even-order mode (TM$_{110}$ at 2.55 GHz) and the first odd-order mode (TM$_{010}$ at 2.64 GHz) can be excited in the second-harmonic band for achieving a wideband
We have conducted full-wave numerical simulations [39] to validate the analytical results. Figs. 3(a)-(c) present snapshots of electric field distributions for the TM$_{310}$, TM$_{e110}$ and TM$_{o110}$ modes, respectively. The simulated field distributions are in good agreement with results obtained from the cavity model, showing that the TM$_{e110}$ and TM$_{o110}$ modes exhibit orthogonal modal patterns.

### III. EXPERIMENTAL RESULTS

According to the theoretical analysis, we have fabricated the dual-band microstrip antenna based on the FR4 substrate and copper (Cu) microstrips, as shown in Fig. 4. The important design parameters are listed in Table I. In particular, it should be noted that a 50 ohms coaxial cable feed is positioned at $x = -5$ mm, $y = 4.5$ mm to simultaneously excite the TM$_{e110}$ (2.55 GHz) and TM$_{o110}$ (2.64 GHz) modes of the elliptical patch. A fluidic cavity with radius $r = 2$ mm is drilled at position $x = -27$ mm and $y = -20$ mm, where the TM$_{310}$ resonant mode exhibits

![Fig. 6. Radiation patterns for the microstrip patch antenna in Fig. 4 on the E- and H-planes at: (a) 1.33 GHz, (b) 2.52 GHz, (c) 2.6 GHz, and (d) 2.69 GHz.](image)

![Fig. 7. Measured reflection spectrum (TM$_{310}$ mode) for the microstrip patch antenna, loaded with the acetone-water mixture at different concentrations; the inset shows the measured and calculated resonance frequency $f_0$ against the volume fraction of water.](image)

<table>
<thead>
<tr>
<th>Mixtures</th>
<th>0 % (acetone)</th>
<th>20%</th>
<th>40%</th>
<th>60%</th>
<th>80%</th>
<th>100 % (water)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\varepsilon'_r$</td>
<td>30.7</td>
<td>20.7</td>
<td>25</td>
<td>35</td>
<td>45</td>
<td>66</td>
</tr>
<tr>
<td>$\varepsilon''_r$</td>
<td>0.5</td>
<td>1</td>
<td>1.65</td>
<td>2.5</td>
<td>4.3</td>
<td>6</td>
</tr>
</tbody>
</table>

![Fig. 8. Measured harmonic RSSI array for the water-acetone mixture (60 %), which was recorded by the spectrum analyzer connected to the sniffer Rx. The envelope of this RSSI array forms the FHSS pattern that contains sensing information for the fully-passive harmonic sensor.](image)
the maximum electric field strength [see Fig. 3(a)]. To accurately control the volume in the microcavity, a fluidic channel consisting of three acrylic layers with thickness \( h_1, h_2 \) and \( h_3 \) was fabricated [see Table I]. Each layer was etched into the specific shape [Fig. 2] by using Epilog Mini 24 laser cutter, and all layers were tied together using the double-sided adhesive tape. Subsequently, the assembled fluidic channel was mounted onto the patch antenna and connected with two plastic tubes (i.e., inlet and outlet) [Fig. 4]. Fig. 5 reports the simulated (solid lines) and measured (dashed lines) reflection coefficients versus frequency for this dual-band microstrip antenna. The resonance frequencies calculated using Eqs. (1) and (2) are also highlighted (red stars) here, which agree well with the full-wave simulation results. This measurement results confirm the dual-band behavior of the antenna, with a reflection dip at 1.33 GHz and a broadband resonance at its doubled frequency (2.5 GHz - 2.7 GHz). Although the harmonic sensor is designed to work in the S-band range (2 - 4 GHz), the concept and design can be readily transferred to other frequency bands. Fig. 6 reports the simulated and measured radiation patterns of the proposed microstrip antenna on the E- and H-planes at the fundamental frequency and the second-harmonic band. Note that for the TM_{310} mode, the E-plane is \( yz \)-plane and the H-plane is \( xz \)-plane in 3D space, and those for the TM_{410} (TM_{410}) modes are \( yz \)- and \( xz \)-planes (\( xz \)- and \( yz \)-planes). The measured co-polarization radiation patterns with broadside radiation properties are in good agreement with the simulation results. At 1.33 GHz (TM_{310} mode), this antenna exhibits a maximum measured gain of -1.5 dBi, with a half-power beam width (HPBW) of 72° on the E-plane and a HPBW of 106° on H-plane. In the second-harmonic band, the TM_{310} mode (2.52 GHz) and TM_{410} mode (2.69 GHz) exhibit orthogonal linear polarizations, whereas circular polarizations are obtained between the two modes (2.6 GHz). At 2.52 GHz, the antenna exhibits a maximum gain of 4.5 dBi, with a HPBW of 84° (120°) on the E-plane (H-plane). At 2.69 GHz, the maximum antenna gain is 5.7 dBi, with a HPBW of 77° (115°) on the E-plane (H-plane). In these two cases, a high copolarization discrimination is apparently seen, with a cross-polarization less than -15 dB (-10 dB) on the E-plane (H-plane). At 2.6 GHz, the antenna shows a maximum gain of 5.3 dBi and a HPBW of 86° (116°) on the E-plane (H-plane). In this case, the cross-polarization radiation pattern is similar to the co-polarization pattern, in light of intrinsic circular polarization properties of the elliptical patch. Due to relatively high dielectric and conduction losses in the FR4 substrate, the measured radiation efficiency is 27 % at 1.31 GHz and is greater than 80 % in the second-harmonic band. The realized gain of the proposed antennas can be further enhanced by selecting a high-quality substrate with minimum power dissipation.

Next, we will demonstrate the sensing function of the proposed reconfigurable dual-band antenna in terms of reflection spectrum. To this end, acetone and water mixtures with various concentrations were prepared with their complex permittivities listed in Table II [40]-[42]. Based on the perturbation theory [43], [44], the dielectric properties of the SUT filled into the fluidic cavity can be characterized by detecting the up- or down-shifting resonance frequency \( f_o \). In this study, to track the resonant frequency variation of the dual-
According to the Friis transmission equation [46], the ratio of the power received by $R_s$ to the power launched by $T_s$ is given by:

$$\frac{P_s}{P_l} = \left(\frac{\lambda_0}{4\pi R_s}\right)^2 \left(\frac{\lambda_0}{2\pi R_i}\right)^2 \frac{G_1 G_2 G_3}{L_{sys}} \left|\hat{\rho}_x \cdot \hat{\rho}_x\right|^2 \left|\hat{\rho}_y \cdot \hat{\rho}_y\right|^2,$$  

(3)

where $G_1$ ($G_2$) is the realized gain of the dual-band antenna on the harmonic sensor at $f_1$ ($2f_1$), $G_T$ ($G_R$) denotes the realized gain of the transceiver (sniffer) used to interrogate the passive sensor, $R_s$ ($R_i$) is the distance between $T_s$ ($R_s$) and the harmonic sensor, $L_{sys}$ is the system loss including the frequency-conversion loss and parasitics. Here, important parameters are: $P_l = 25$ dBm, $R_s = 2$ m, $G_T = 5.5$ dBi at 1.1 GHz and $G_R = 12$ dBi at 2.6 GHz. In Eq. (3), $\left|\hat{\rho}_x \cdot \hat{\rho}_x\right|^2$ is the polarization coupling factor between the $T_s$ antenna and the harmonic sensor, which is approximately equal to unity if the two antennas are well aligned. On the other hand, $\left|\hat{\rho}_y \cdot \hat{\rho}_y\right|^2$ accounts for the polarization match between the $R_s$ antenna and the harmonic sensor. Since the TM$_{110}$ mode and TM$_{210}$ modes excited in the second-harmonic band have orthogonal polarizations [see Figs. 3 and 6], the $R_s$ antenna is tilted by $45^\circ$ to capture radiation produced by both modes; here, $\left|\hat{\rho}_x \cdot \hat{\rho}_x\right|^2$ is $\sim 50\%$ in the entire second-harmonic band. In summary, according to Eq. (3), the received power $P_s$ and RSSI are proportional to the realized gain $G_1$ and $G_2$, in which $G_2$ remains almost constant with a $\pm 0.5$ dB fluctuation, while $G_1$ is quite sensitive to the concentration of the acetone-water mixture. When the acetone concentration decreases, which is corresponding to the increase of the dielectric constant of the mixture, the frequency of peak $G_1$ is shifted from 1.325 GHz to 1.287 GHz [see Fig. 7], leading to the FHSS pattern downshift as can be seen in Fig. 9(c) (measured in an anechoic chamber) and Fig. 9(d) (measured in a rich-scattering indoor environment). It is evidently seen that the peak RSSI of FHSS pattern is sensitively shifted from 2.642 GHz to 2.58 GHz and that such a trend is independent of the density of the electromagnetic environment. In this work, for comparison, we also employed the conventional passive backscatter sensor to wirelessly monitor the same liquid mixtures. In this case, the dual-band microstrip antenna is disconnected from the frequency doubler and its port 1 (labeled in Fig. 2(b)) is terminated by a $50\,\Omega$ match load. We notice that in passive scattering events, the extinction cross section is the sum of absorption and scattering cross sections. A dip in RSSI and RCS spectrum is sometimes observed at the resonance. In this case, the incident power is absorbed without causing too much scattering; namely, the absorption cross section is greater than the scattering cross section [47]. Figs. 9(e) and 9(f) report the measured FHSS pattern for the conventional backscatter sensor placed in the anechoic chamber and the noisy environment, respectively. Although the backscatter sensor can function well in a noise-free anechoic chamber, it fails to comprehensively detect the liquid properties in rich-scattering environments.

Fig. 10. Experimental setup in rich-scattering indoor environment with (a) two more metal reflectors and (b) six metal reflectors. (c) Peak frequency against the volume fraction of water in the acetone-water mixture; here, data was obtained using the harmonic sensor placed in different environments including Figs. 9(a) and 9(b).
environments involving echoes, clutters, multipath scattering, and the possible crosstalk between $T_c$ and $R_c$. Apparently, compared to conventional backscatter sensors, our proposed frequency-hopping harmonic sensor can robustly and sensitively detect dielectric properties of liquid mixtures, regardless of background interferences. Fig. 10 summarizes the measured peak values of FHSS pattern as a function of the water volume fraction in different scattering-rich environments. It is evident that increasing the number of large PEC scatters surrounding the harmonic sensor would not affect the sensing performance, which further demonstrates the robustness and effectiveness of our frequency-hopping harmonic sensor. Moreover, we can define our sensitivity as the slope of the curve, i.e., $-0.62$ MHz/1%, which means when the volume fraction of water is increased by 1%, the peak of the FHSS pattern will be downshifted by 0.62 MHz. Such sensitivity and resolvability allow us to differentiate two liquids with a difference of 5% water.

Finally, we have validated the repeatability and real time capability (transient response) of this harmonic sensor working in a noisy environment. Here, different acetone-water mixtures were injected in and removed from the fluidic cavity every minute, with a 30 s interval for the empty state reference. The measurement results reported in Fig. 11 clarify that the sensor can always restore to its original state (with a peak RSSI at 2.66 GHz) after several operating cycles. Such a robust and repeatable wireless sensing capability may enable many biological and healthcare monitoring applications, such as the wireless passive lab-on-chip platforms. We should also note that the proposed compact harmonic sensor may be integrated with more complex fluidic channels and diagnostic assays to maximize its potential for high-performance wireless sensing and telemetering.

IV. CONCLUSION

We have proposed a low-profile, reconfigurable dual-band microstrip antenna for realizing far field wireless frequency-hopping harmonic sensors. The proposed microstrip antenna, loaded appropriately with a fluidic channel, can exhibit a tunable narrow resonance at the fundamental frequency and an invariant wideband resonance at the second-harmonic frequency. We have demonstrated that such an antenna is particularly useful for the frequency-hopping telemetry scheme, which allows for robust wireless liquid sensing in noisy environments (e.g., dense urban and indoor areas). The implementation of compact zero-power harmonic sensors with the capability of noise suppression may pave the way towards future integrated IoT sensors and battery-less smart RFID tags.

REFERENCES
