

# OUTLINE

- Documents
- Terms
  - General + Non-English
  - English
- Skip pointers
- Phrase queries

# Phrase queries

- We want to answer a query such as [stanford university] – as a phrase.
- Thus *The inventor Stanford Ovshinsky never went to university* should **not** be a match.
- The concept of phrase query has proven easily understood by users.
- About 10% of web queries are phrase queries.
- Consequence for inverted index: it no longer suffices to store docIDs in postings lists.
- Two ways of extending the inverted index:
  - biword index
  - positional index

# Biword indexes

- Index every consecutive pair of terms in the text as a phrase.
- For example, “*Friends, Romans, Countrymen*” would generate two biwords: “*friends romans*” and “*romans countrymen*”
- Each of these biwords is now a vocabulary term.
- Two-word phrases can now easily be answered.

# Longer phrase queries

- A long phrase like “*stanford university palo alto*” can be represented as the Boolean query “**STANFORD UNIVERSITY**” AND “**UNIVERSITY PALO**” AND “**PALO ALTO**”
- We need to do post-filtering of hits to identify subset that actually contains the 4-word phrase.

# Extended biwords

- Parse each document and perform part-of-speech tagging
- Classify the terms into (say) nouns (N) and articles/prepositions (X), and others...
- Now deem any string of terms of the form  $NX^*N$  to be an *extended biword* (actually a *proper noun*)
- Examples: **catcher in the rye**

N X X N

**king of Denmark**

N X N

- Include extended biwords in the term vocabulary
- Queries are processed accordingly

# Issues with biword indexes

## Why are biword indexes rarely used?

- False positives
- Index **blowup** due to very large term vocabulary

Quiz: Can you provide one example of false positive when using a biword index?

# Positional indexes

- Positional indexes are a more efficient alternative to biword indexes.
- Postings lists in a **nonpositional** index: each posting is just a docID
- Postings lists in a **positional** index: each posting is a docID and **a list of positions**

# Positional indexes: Example

Query: “ $to_1 be_2 or_3 not_4 to_5 be_6$ ”

TO, 993427:

1: <7, 18, 33, 72, 86, 231>;

2: <1, 17, 74, 222, 255>;

4: <8, 16, 190, 429, 433>;

5: <363, 367>;

7: <13, 23, 191>; . . . >

BE, 178239:

1: <17, 25>;

4: <17, 191, 291, 430, 434>;

5: <14, 19, 101>; . . . >

**Document 4 is a match!**

## Quiz: Positional index

What is the time complexity of doing a phrasal query of length  $K$  on a positional index of  $D$  documents with max document length of  $L$ , and a dictionary of size  $V$ ?

# Proximity search

- We just saw how to use a positional index for phrase searches.
- We can also use it for proximity search.
- For example: employment /4 place
- Find all documents that contain EMPLOYMENT and PLACE within 4 words of each other.
- *Employment agencies that place healthcare workers are seeing growth* is a hit.
- *Employment agencies that have learned to adapt now place healthcare workers* is not a hit.

# Proximity search

- Use the positional index
- Simplest algorithm: look at cross-product of positions of (i) EMPLOYMENT in document and (ii) PLACE in document
- Very inefficient for frequent words, especially stop words
- Note that we want to return the actual matching positions, not just a list of documents.
- This is important for dynamic summaries etc.

# “Proximity” intersection

```
POSITIONALINTERSECT( $p_1, p_2, k$ )
1  answer  $\leftarrow \langle \rangle$ 
2  while  $p_1 \neq \text{NIL}$  and  $p_2 \neq \text{NIL}$ 
3  do if  $\text{docID}(p_1) = \text{docID}(p_2)$ 
4      then  $l \leftarrow \langle \rangle$ 
5           $pp_1 \leftarrow \text{positions}(p_1)$ 
6           $pp_2 \leftarrow \text{positions}(p_2)$ 
7          while  $pp_1 \neq \text{NIL}$ 
8          do while  $pp_2 \neq \text{NIL}$ 
9              do if  $|\text{pos}(pp_1) - \text{pos}(pp_2)| \leq k$ 
10                 then  $\text{ADD}(l, \text{pos}(pp_2))$ 
11                 else if  $\text{pos}(pp_2) > \text{pos}(pp_1)$ 
12                     then break
13                      $pp_2 \leftarrow \text{next}(pp_2)$ 
14                 while  $l \neq \langle \rangle$  and  $|l[0] - \text{pos}(pp_1)| > k$ 
15                 do  $\text{DELETE}(l[0])$ 
16                 for each  $ps \in l$ 
17                 do  $\text{ADD}(\text{answer}, \langle \text{docID}(p_1), \text{pos}(pp_1), ps \rangle)$ 
18                  $pp_1 \leftarrow \text{next}(pp_1)$ 
19                  $p_1 \leftarrow \text{next}(p_1)$ 
20                  $p_2 \leftarrow \text{next}(p_2)$ 
21             else if  $\text{docID}(p_1) < \text{docID}(p_2)$ 
22                 then  $p_1 \leftarrow \text{next}(p_1)$ 
23                 else  $p_2 \leftarrow \text{next}(p_2)$ 
24 return answer
```

# Combination scheme

- Biword indexes and positional indexes can be profitably combined.
- Many biwords are extremely frequent: Michael Jackson, Britney Spears etc.
- For these biwords, increased speed compared to positional postings intersection is substantial.
- Combination scheme: Include frequent biwords as vocabulary terms in the index. Do all other phrases by positional intersection.
- Williams et al. (2004) evaluate a more sophisticated mixed indexing scheme. Faster than a positional index, at a cost of 26% more space for index.

# “Positional” queries on Google

- For web search engines, positional queries are much more expensive than regular Boolean queries.
- Why are they more expensive than regular Boolean queries?
- Can you demonstrate on Google that phrase queries are more expensive than Boolean queries?
- Let's look at some examples of phrase queries.



"New York University"



All Images Maps News Videos More Settings Tools

About 118,000,000 results (1.35 seconds)

NYU

<https://www.nyu.edu/>

Founded in 1831 to enlarge the scope of higher education: includes thirteen schools, colleges, and divisions at five major centers in Manhattan.

Results from nyu.edu



**Undergraduate Admissions**

How to Apply - Majors and Programs - Aid and Costs - ...

**Admissions**

Undergraduate Admissions - Graduate Admissions - Fall in NY

**Graduate Admissions**

At the graduate level, each school has its own, separate ...

**Academic Programs**



New York University



All Images Maps News Videos More Settings Tools

About 1,040,000,000 results (1.17 seconds)

NYU

<https://www.nyu.edu/>

Founded in 1831 to enlarge the scope of higher education: includes thirteen schools, colleges, and divisions at five major centers in Manhattan.

Results from nyu.edu



**Undergraduate Admissions**

How to Apply - Majors and Programs - Aid and Costs - ...

**Admissions**

Undergraduate Admissions - Graduate Admissions - Fall in NY

**Visit NYU**

Visit NYU Because Seeing is Believing ... of the NYU ...

**Graduate Admissions**

At the graduate level, each school has its own, separate ...

**About NYU**

About NYU. In 1831, Albert Gallatin, the distinguished ...

**NYU Stern**

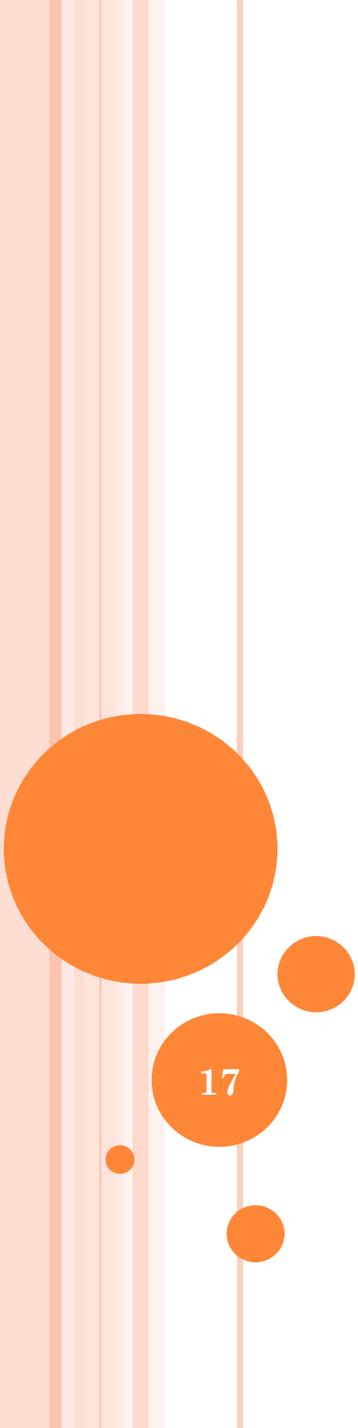
Explore the NYU Stern School of Business and learn more about ...

# Take-away

- Understanding of the basic unit of classical information retrieval systems: **words** and **documents**: What is a document, what is a term?
- Tokenization: how to get from raw text to words (or tokens)
- More complex indexes: skip pointers and phrases

# Resources

- Chapter 1 and 2 of IIR
- Resources at <https://tartarus.org/martin/PorterStemmer/>
  - Porter stemmer



# DICTIONARY & TOLERANT RETRIEVAL

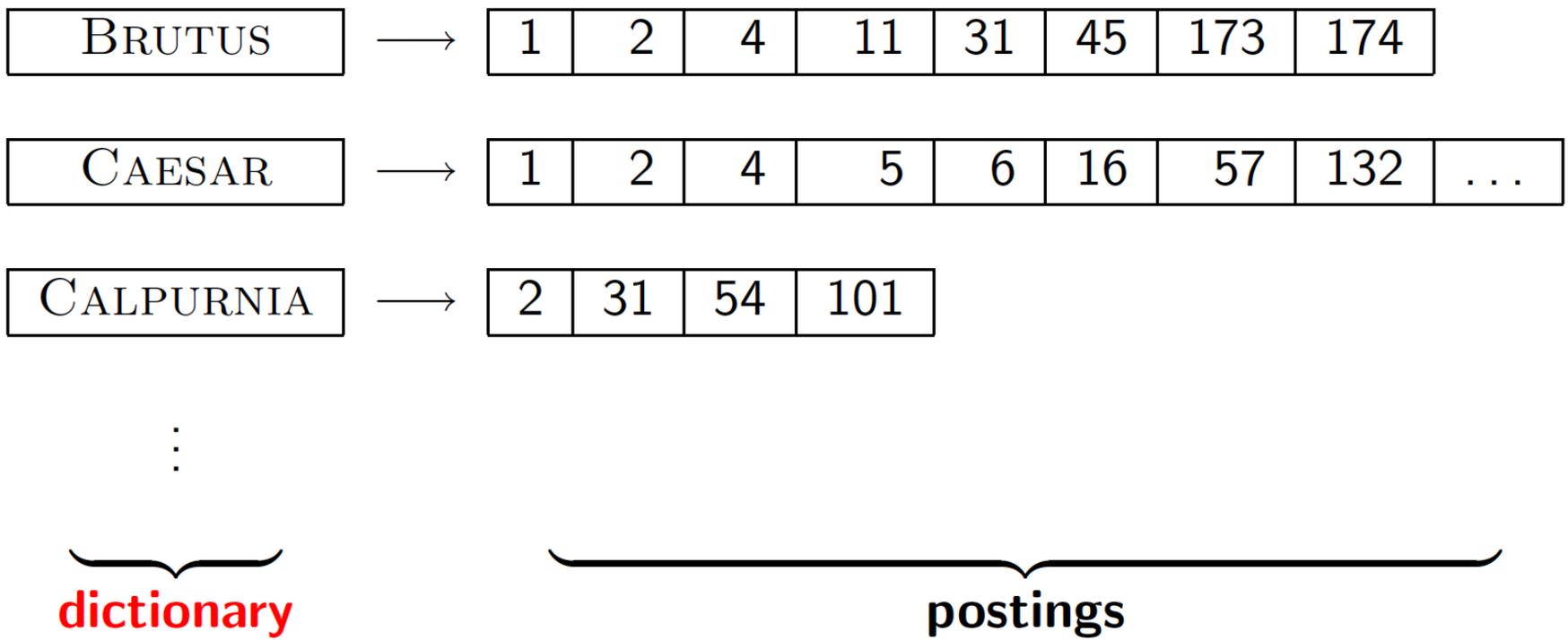
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## THIS LECTURE

- Dictionary data structures
- “Tolerant” retrieval
  - Wild-card queries
  - Spelling correction
  - Soundex

# DICTIONARY DATA STRUCTURES FOR INVERTED INDEXES

- The dictionary data structure stores the term vocabulary, document frequency, pointers to each postings list ... **in what data structure?**



# A NAÏVE DICTIONARY

- An array of struct:

term	document frequency	pointer to postings list
a	656,265	→
aachen	65	→
...	...	...
zulu	221	→

char[20]    int    Postings \*

20 bytes    4/8 bytes    4/8 bytes

- How do we store a dictionary in memory efficiently?
- How do we quickly look up elements at query time?

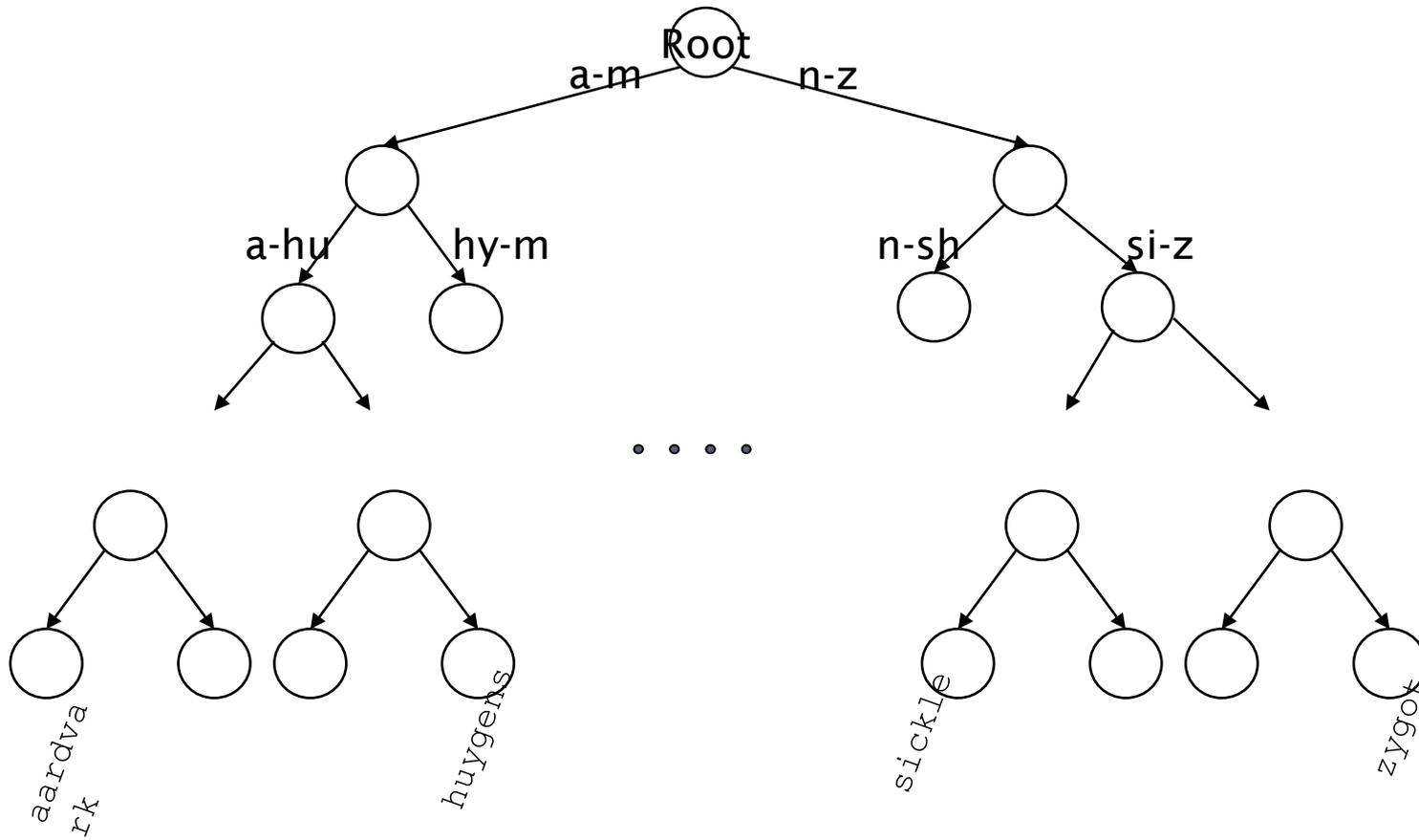
# DICTIONARY DATA STRUCTURES

- Two main choices:
  - Hashtables
  - Trees
- Some IR systems use hashtables, some trees

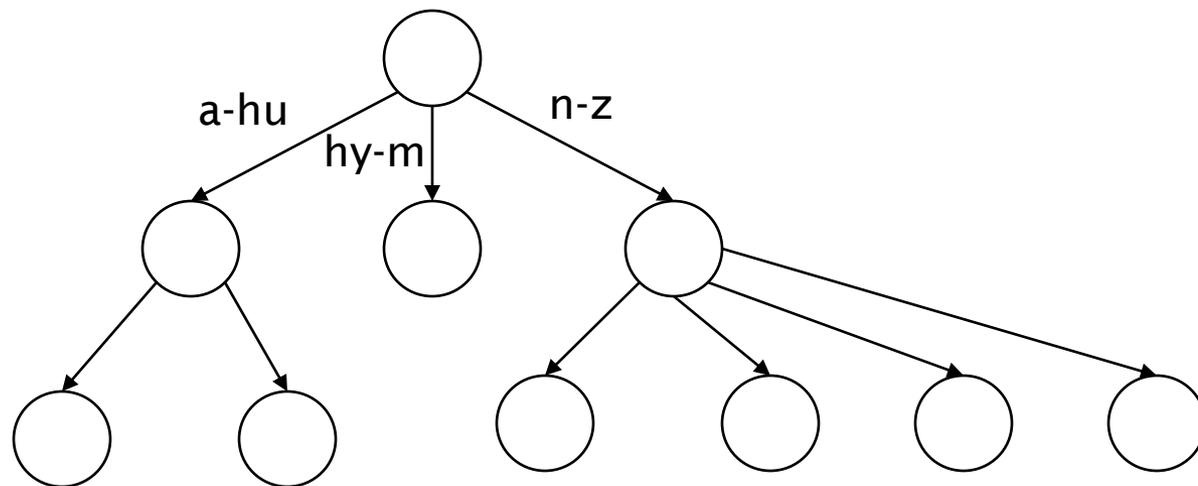
# HASHTABLES

- Each vocabulary term is hashed to an integer
  - (We assume you've seen hashtables before)
- Pros:
  - Lookup is faster than for a tree:  $O(1)$
- Cons:
  - No easy way to find minor variants:
    - judgment/judgement
  - No prefix search [tolerant retrieval]
  - If vocabulary keeps growing, need to occasionally do the expensive operation of rehashing *everything*
    - Due to bucket overflow!

# TREE: BINARY TREE



# TREE: B-TREE



- Definition: Every internal node has a number of children in the interval  $[a, b]$  where  $a, b$  are appropriate natural numbers, e.g.,  $[2, 4]$ .
- The range has to do with the size of a disk block or memory page, which stores one node

# TREES

- Simplest: binary tree
- More usual: B-trees
- Trees require a standard ordering of characters and hence strings ... but we typically have one
- Pros:
  - Solves the prefix problem (terms starting with *hyp*)
- Cons:
  - Slower:  $O(\log M)$  [and this requires *balanced* tree]
  - Rebalancing binary trees is expensive
    - But B-trees mitigate the rebalancing problem

## WILD-CARD QUERIES: \*

- ***mon\****: find all docs containing any word beginning with “mon”.
- Easy with binary tree (or B-tree) lexicon: retrieve all words in range: ***mon***  $\leq w <$  ***moo***
- ***\*mon***: find words ending in “mon”: harder
  - Maintain an additional B-tree for terms *backwards*.  
Can retrieve all words in range: ***nom***  $\leq w <$  ***non***.

## QUIZ: ENUMERATION

From the last slide, how can we enumerate all terms satisfying the wild-card query

*de\*cy* ?

## QUERY PROCESSING

- At this point, we have an enumeration of all terms in the dictionary that match the wild-card query.
- We still have to look up the postings for each enumerated term.
- E.g., consider the query:

***se\*ate AND fil\*er***

This may result in the execution of many Boolean *AND* queries.

## B-TREES HANDLE \*'S AT THE END OF A QUERY TERM

- How can we handle \*'s in the middle of query term?
  - *co\*tion*
- We could look up *co\** AND *\*tion* in a B-tree and intersect the two term sets
  - Expensive
- The solution: transform wild-card queries so that the \*'s occur at the end
- This gives rise to the **Permuterm** Index.

# PERMUTERM INDEX

- For term *hello*, index under:
  - *hello\$, ello\$h, llo\$he, lo\$hel, o\$hell, \$hello*  
where \$ is a special symbol (end of a term).
- Queries:
  - **X** lookup on **X\$**                      **X\*** lookup on **\$X\***
  - **\*X** lookup on **X\$\***                      **\*X\*** lookup on **X\***
  - **X\*Y** lookup on **Y\$X\***

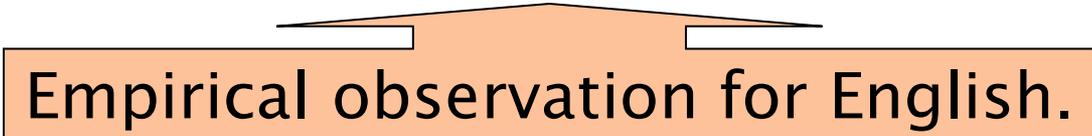
  
 Query = *hel\*o*  
*X=hel, Y=o*  
 Lookup *o\$hel\**

## QUIZ: PERMUTERM

1. Using PermuTerm Index, how do we answer query “**\*tion\***” ?
2. How do we answer query **X\*Y\*Z?**

## PERMUTERM QUERY PROCESSING

- Rotate query wild-card to the right
- Now use B-tree lookup as before.
- *Permuterm problem:  $\approx$  quadruples lexicon size*



Empirical observation for English.

## BIGRAM ( $K$ -GRAM) INDEXES

- Enumerate all  $k$ -grams (sequence of  $k$  chars) occurring in any term
- e.g., from text “*April is the cruelest month*” we get the 2-grams (*bigrams*)

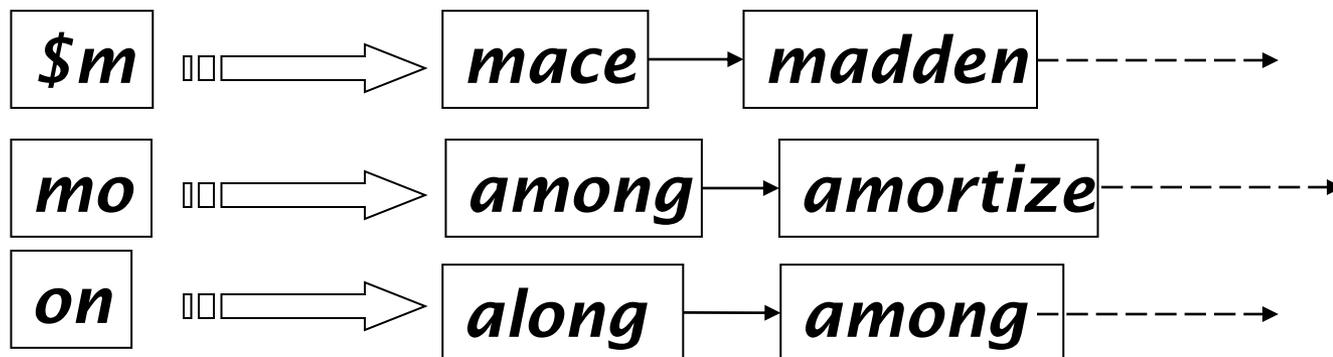
\$a,ap,pr,ri,il,l\$, \$i,is,s\$, \$t,th,he,e\$, \$c,  
cr,ru,

ue,el,le,es,st,t\$, \$m,mo,on,nt,h\$

- \$ is a special word boundary symbol
- Maintain a second inverted index from bigrams to dictionary terms that match each bigram.

## BIGRAM INDEX EXAMPLE

- The  $k$ -gram index finds *terms* based on a query consisting of  $k$ -grams (here  $k=2$ ).



## PROCESSING WILD-CARDS

- Query *mon\** can now be run as
  - *\$m AND mo AND on* 
- Gets terms that match and AND them.
- But we would enumerate *moon*.
- Must post-filter these terms against query.
- Surviving enumerated terms are then looked up in the term-document inverted index.
- Fast, space efficient (compared to permuterm).

## PROCESSING WILD-CARD QUERIES

- As before, we must execute a Boolean query for each enumerated, filtered term.
- Wild-cards can result in expensive query execution (very large disjunctions...)
  - `pyth*` AND `prog*`
- If you encourage “laziness” people will respond!

Type your search terms, use '\*' if you need to.  
E.g., `Alex*` will match Alexander.

- Which web search engines allow wildcard queries?

# SPELL CORRECTION

- Two principal uses
  - Correcting document(s) being indexed
  - Correcting user queries to retrieve “right” answers
- Two main flavors:
  - Isolated word
    - Check each word on its own for misspelling
    - Will not catch typos resulting in correctly spelled words
    - e.g., *from* → *form*
  - Context-sensitive
    - Look at surrounding words,
    - e.g., *I flew form Heathrow to Narita.*

# DOCUMENT CORRECTION

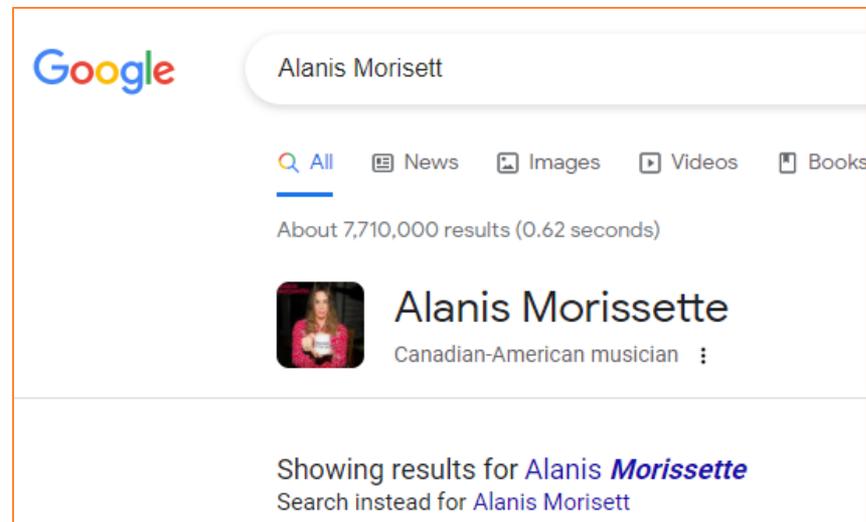
- Especially needed for OCR'ed documents
  - Correction algorithms are tuned for this: rn vs. m
  - Can use domain-specific knowledge
    - E.g., OCR can confuse O and D more often than it would confuse O and I (adjacent on the QWERTY keyboard, so more likely interchanged in typing).
- But also: web pages and even printed material have typos (some docs ASR'ed)
- Goal: the dictionary contains fewer misspellings
- But often we don't change the documents and instead fix the query-document mapping

# QUIZ: MISSPELLINGS

- Suggest reasons for the following misspellings:
  - acwuire (acquire)
  - ornit (omit)
  - section (sanction)

# QUERY MIS-SPELLINGS

- Our principal focus here
  - E.g., the query *Alanis Morisett*
- We can either
  - Retrieve documents indexed by the correct spelling, OR
  - Return several suggested alternative queries with the correct spelling
    - *Did you mean ... ?*



# ISOLATED WORD CORRECTION

- Fundamental premise – there is a lexicon from which the correct spellings come
- Two basic choices for this
  - A standard lexicon such as
    - Webster's English Dictionary
    - An “industry-specific” lexicon – hand-maintained
  - The lexicon of the indexed corpus
    - E.g., all words on the web
    - All names, acronyms etc.
    - (Including the mis-spellings)

## ISOLATED WORD CORRECTION

- Given a lexicon and a character sequence  $Q$ , return the words in the lexicon closest to  $Q$
- What's "closest"?
- We'll study several alternatives
  - Edit distance (Levenshtein distance)
  - Weighted edit distance
  - $n$ -gram overlap

## EDIT DISTANCE

- Given two strings  $S_1$  and  $S_2$ , the minimum number of operations to convert one to the other
- Operations are typically character-level
  - Insert, Delete, Replace, (Transposition)
- E.g., the edit distance from **dof** to **dog** is 1
  - From **cat** to **act** is 2 (Just 1 with transpose.)
  - from **cat** to **dog** is 3.
- Generally found by dynamic programming.
- See <http://www.let.rug.nl/kleiweg/lev/> for a nice example plus an applet.

## QUIZ: EDIT DISTANCE

- Considering only insertion, deletion and replacement, what is the edit distance:

1) gap → apply

2) goat → toad

3) sonne → sony

## WEIGHTED EDIT DISTANCE

- As above, but the weight of an operation depends on the character(s) involved
  - Meant to capture OCR or keyboard errors  
Example: *m* more likely to be mis-typed as *n* than as *q*
  - Therefore, replacing *m* by *n* is a smaller edit distance than by *q*
  - This may be formulated as a probability model:  
$$P(n \mid m)$$
- Requires weight matrix as input
- Modify dynamic programming to handle weights

## USING EDIT DISTANCES

- Given query, first enumerate all character sequences within a preset (weighted) edit distance (e.g., 2)
- Intersect this set with list of “correct” words
- Show terms you found to user as suggestions
- Alternatively,
  - We can look up all possible corrections in our inverted index and return all docs ... slow
  - We can run with a single most likely correction
- The second alternative disempowers the user, but saves a round of interaction with the user

# EDIT DISTANCE TO ALL DICTIONARY TERMS?

- Given a (mis-spelled) query – do we compute its edit distance to every dictionary term?
  - Expensive and slow
  - Alternative?
    - generate everything up to edit distance  $k$  and then intersect.
    - Fine for distance 1; okay for distance 2.
- How do we cut down the set of candidate dictionary terms?
- One possibility is to use  $n$ -gram overlap for this
- This can also be used by itself for spelling correction.

## N-GRAM OVERLAP

- Enumerate all the  $n$ -grams in the query string as well as in the lexicon
- Use the  $n$ -gram index (recall wild-card search) to retrieve all lexicon terms matching any of the query  $n$ -grams
- Threshold by number of matching  $n$ -grams
  - Variants – weight by keyboard layout, etc.

## EXAMPLE WITH TRIGRAMS

- Suppose the text is ***november***
  - Trigrams are *nov, ove, vem, emb, mbe, ber.*
- The query is ***december***
  - Trigrams are *dec, ece, cem, emb, mbe, ber.*
- So 3 trigrams overlap (of 6 in each term)
- The amount overlap indicates the similarity between query and the text
- How can we turn this into a normalized measure of overlap?

## ONE OPTION – JACCARD COEFFICIENT

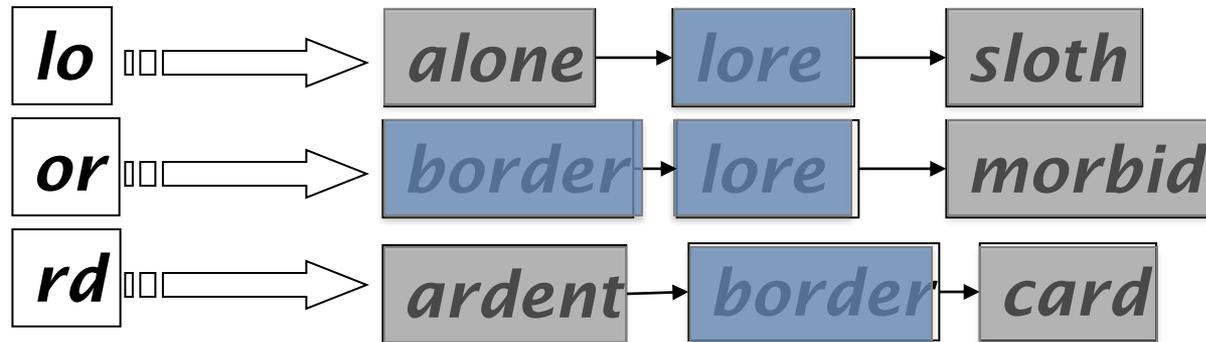
- A commonly-used measure of overlap
- Let  $X$  and  $Y$  be two sets; then the J.C. is

$$|X \cap Y| / |X \cup Y|$$

- Equals 1 when  $X$  and  $Y$  have the same elements and zero when they are disjoint
- $X$  and  $Y$  don't have to be of the same size
- Always assigns a number between 0 and 1
  - Now threshold to decide if you have a match
  - E.g., if J.C.  $> 0.8$ , declare a match

## MATCHING TRIGRAMS

- Consider the query *lord* – we wish to identify words matching 2 of its 3 bigrams (*lo*, *or*, *rd*)



Standard postings “merge” will enumerate ...

Adapt this to using Jaccard (or another) measure.

## CONTEXT-SENSITIVE SPELL CORRECTION

- Text: *I flew from Heathrow to Narita.*
- Consider the phrase query “*flew form Heathrow*”
- We’d like to respond  
Did you mean “*flew from Heathrow*”?  
because no docs matched the query phrase.

## CONTEXT-SENSITIVE CORRECTION

- Need surrounding context to catch this.
- First idea: retrieve dictionary terms close (in weighted edit distance) to each query term
- Now try all possible resulting phrases with one word “corrected” at a time
  - *flew from heathrow*
  - *fled form heathrow*
  - *flea form heathrow*
- **Hit-based spelling correction:** Suggest the alternative that has lots of hits.

## QUIZ: SPELL CORRECTION

- Suppose that for “*flew form Heathrow*” we have 4 alternatives for flew, 5 for form and 6 for heathrow.

How many “corrected” phrases will we enumerate in this scheme?

## ANOTHER APPROACH

- Break phrase query into a conjunction of biwords (Previous lecture).
- Look for biwords that need only one term corrected.
- Enumerate only phrases containing “common” biwords.

## GENERAL ISSUES IN SPELL CORRECTION

- We enumerate multiple alternatives for “Did you mean?”
- Need to figure out which to present to the user
  - The alternative hitting most docs
  - Query log analysis
- More generally, rank alternatives probabilistically

$$\operatorname{argmax}_{corr} P(corr \mid query)$$

- From Bayes rule, this is equivalent to

$$\operatorname{argmax}_{corr} P(query \mid corr) * P(corr)$$

Noisy channel

Language model

# SOUNDEX

- Class of heuristics to expand a query into **phonetic** equivalents
  - Language specific – mainly for names
  - E.g., *chebyshev* → *tchebycheff*
- Invented for the U.S. census ... in 1918

## SOUNDEX – TYPICAL ALGORITHM

- Turn every token to be indexed into a 4-character reduced form
- Do the same with query terms
- Build and search an index on the reduced forms
  - (when the query calls for a soundex match)
- Details can be found:  
<http://www.creativyst.com/Doc/Articles/SoundEx1/SoundEx1.htm#Top>

## SOUNDEX – TYPICAL ALGORITHM

1. Retain the first letter of the word.
2. Change all occurrences of the following letters (vowels and alike) to '0' (zero):  
'A', 'E', 'I', 'O', 'U', 'H', 'W', 'Y'.
3. Change letters to digits as follows (equivalence classes):
  - B, F, P, V  $\rightarrow$  1
  - C, G, J, K, Q, S, X, Z  $\rightarrow$  2
  - D, T  $\rightarrow$  3
  - L  $\rightarrow$  4
  - M, N  $\rightarrow$  5
  - R  $\rightarrow$  6

To be continued...

## SOUNDEX (CONTINUED)

4. Retain the first digit if two identical digits are side-by-side
5. Remove all zeros from the resulting string.
6. Pad the resulting string with trailing zeros and return the first four positions, which will be of the form <uppercase letter> <digit> <digit> <digit>.

E.g., *Herman* → H06505 → H655.

Will *hermann* generate the same code?

## QUIZ: SOUNDEX

- Which of the following is NOT true about soundex:
  - a) The first letter of the code is capitalized
  - b) There is no zero's in the code
  - c) There are exactly 4 letters in a code
  - d) All letter except for the first are numerical digits

# SOUNDEX

- Soundex is the classic algorithm, provided by most databases (Oracle, Microsoft, ...)
- How useful is soundex?
- Not very – for information retrieval
- Okay for “high recall” tasks (e.g., Interpol), though biased to names of certain nationalities
- Zobel and Dart (1996) show that other algorithms for phonetic matching perform much better in the context of IR

# WHAT QUERIES CAN WE PROCESS?

- We have
  - Positional inverted index with skip pointers
  - Wild-card index
  - Spell-correction
  - Soundex
- Queries such as  
*(SPELL(moriset) /3 toron\*to) OR SOUNDEX(chaikofski)*

# RESOURCES

- IIR 3, MG 4.2
- Efficient spell retrieval:
  - K. Kukich. Techniques for automatically correcting words in text. ACM Computing Surveys 24(4), Dec 1992.
  - J. Zobel and P. Dart. Finding approximate matches in large lexicons. Software - practice and experience 25(3), March 1995. <http://citeseer.ist.psu.edu/zobel95finding.html>
  - Mikael Tillenius: Efficient Generation and Ranking of Spelling Error Corrections. Master's thesis at Sweden's Royal Institute of Technology. <http://citeseer.ist.psu.edu/179155.html>
- **Nice, easy reading on spell correction:**
  - Peter Norvig: How to write a spelling corrector  
<http://norvig.com/spell-correct.html>