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# Social Media Information Diffusion with ProfileRank

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Shenghan Yu  
Stu. ID. 515030910562

## Abstract

1 With the development of Internet, there have been more and more algorithms  
2 on the rank of webpages. Focusing on the reference relationship proves to be an  
3 effective way to help people find relative important webpages, like PageRank and  
4 HIPS algorithms. In the field of social media, ProfileRank uses similar methods to  
5 deal with information diffusion by identifying influential users and relevant content.  
6

## 7 1 Introduction

8 Nowadays, social media is taking over traditional media. Social media has a far higher speed to  
9 create information, and this feature is very similar to Internet. Therefore, how to identify useful  
10 information becomes a critical problem. It is an important step towards the design of information  
11 diffusion mechanisms, recommendation system, and viral marketing campaigns.

12  
13 Since the information diffusion in the social media is similar to the one on the internet.  
14 We can try to use similar algorithm to deal with the data. On the other way, users have a more  
15 important level in the social media. Every user can create and spread content, and for each time,  
16 there is always one piece of content for one user creating or spreading. Therefore, the key factors in  
17 social media information diffusion are influential users and relevant content.  
18

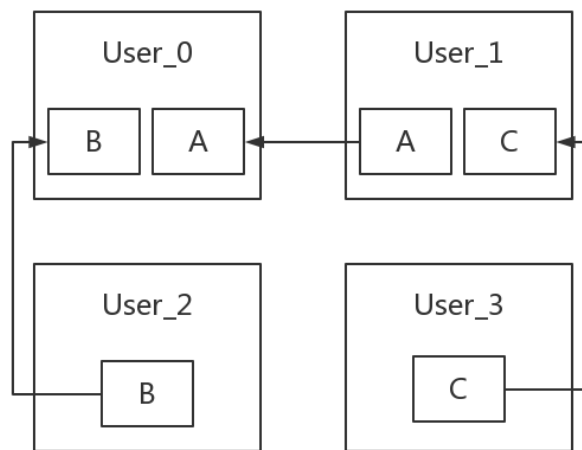


Figure 1: A typical content relationship graph in Twitter.

19 **2 Methodology**

20 ProfileRank considers both influential users and relevant content so that there are two relation  
 21 matrixes which can be extracted from the original data, a user-content matrix  $M$  and a content-user  
 22 matrix  $L$ . There is also a bipartite graph  $G(U, C, F, E)$  from the original data, where  $U$  is the user  
 23 set,  $C$  is the content set, and  $E$  and  $F$  are sets of edges that related users to content and the other way  
 24 around. For Figure 1, the bipartite graph  $G$  can be shown as follow:  
 25

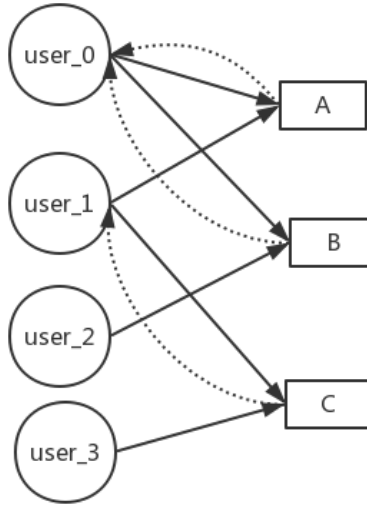


Figure 2: The bipartite graph  $G$  for Figure 1.

26  
 27 The user-content matrix  $M = (m_{i,j})$  is a  $|U| \times |C|$  matrix where  $m_{i,j} = \frac{1}{q_i}$  and  $q_i$  is the number of  
 28 pieces of content the users  $u_i$  has created or propagated. The content-user matrix  $L = (l_{i,j})$  is a  
 29  $|C| \times |U|$  matrix where  $l_{i,j} = 1$  if the user  $u_j$  created the piece of content  $c_i$  and  $l_{i,j} = 0$ , otherwise.  
 30 For the data from Figure 1, the matrix  $M$  and  $L$  can be written as:  
 31

$$M = \begin{bmatrix} \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ 1 & 1 & 1 \end{bmatrix}$$

$$L = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$

32  
 33 At the same time, to make use of these two matrixes, there is a principle: *A piece of content  $c$  is*  
 34 *relevant to a user  $u$  if it is created and propagated by users that are influential to  $u$  and a user  $v$  is*  
 35 *influential to  $u$  if  $v$  creates content that is relevant to  $u$ .* We can get the relationship between content  $r$   
 36 and users  $i$  with this principle.  
 37

$$r = iM$$

$$i = rL$$

38

39 Like PageRank, there are two possible issues: dangling users and buckets. A dangling user never  
40 propagates content from other users. We create an edge  $(u, c)$  from every dangling user to a ghost  
41 piece of content  $c$  and add an edge  $(c, u)$  from the ghost content to all the users. In Figure 1,  $user_0$  is  
42 the dangling user so that the Figure 2 will become the graph shown as follow:

43

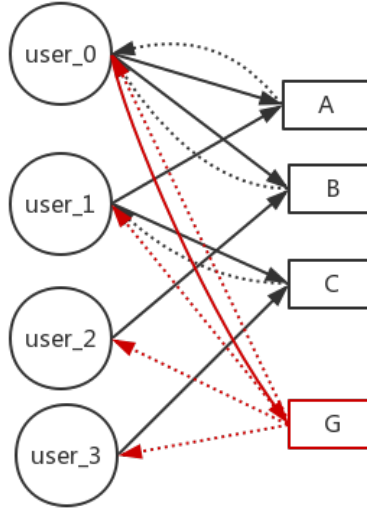


Figure 3: The bipartite graph  $G$  handling dangling users.

44

45 A bucket is a strongly connected subgraph of the bipartite graph. By defining a damping factor  $d$ , the  
46 random tweeter will teleport from current to a random profile. Therefore, the definition of  $r$  and  $i$  can  
47 be modified as:

48

$$r = (1 - d)u(I - dLM)^{-1}$$

$$i = (1 - d)u(I - dML)^{-1}$$

49

50 ProfileRank computes user influence and content relevance based on a user-content bipartite directed  
51 graph, instead of the directed graph employed by PageRank and HITS. ProfileRank's graph is  
52 represented by two matrices, a user-content  $M$  and a content-user  $L$  matrix, and enables the  
53 computation of different score functions, influence and relevance, for different types of nodes, users  
54 and content, based on diffusion data.

55

### 56 3 Conclusion and Future Work

57 ProfileRank is an effective information diffusion model that measures content relevance and user  
58 influence in the bipartite graph. This model takes the unique features in the social media into  
59 consideration, which is also similar to the algorithms for webpages.

60

61 The key factors for ProfileRank are the two relation matrixes. However, the definition of  
62 two matrixes, especially for the user-content matrix, is not very clear, so that there might be a  
63 few problems in the calculation formula. I think that the user-content matrix may be rewrite as:

64  $M = (m_{i,j})$  is a  $|U| \times |C|$  matrix where  $m_{i,j} = \frac{1}{q_i}$  and  $q_i$  is the number of pieces of content the  
65 users  $u_i$  has created or propagated if the user  $u_i$  created or propagated the piece of content  $c_j$ , and  
66  $q_{i,j} = 0$ , otherwise. In this way, the relationship between user and content can be defined more  
67 clearly, and the following formula can also be rewrote as the future work.  
68

#### 69 **4 Reference**

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