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# Modeling Information Diffusion in Multi-Sensitive Networks

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1896

1920

1987

2006

**Time Line:**

**6 weeks reading papers**

**6 weeks proposing a new model and trying to prove it**



**Introduction:**

**Information Diffusion in online social networks**

**Epidemic spread model**

**Learning algorithms**



## **Considering this phenomenon:**

**Sometimes the famous answerers (e.g. Zhang Jiawei and Ma Qianzu) answered a question totally wrong from the professional perspective, but still received lots of likes. Public sees that you have lots of fans, than they think that your answer is right, and vote for it.**



**So, that's what I'm going to find. I think the rate of information diffusion will change with the number of edges a transmit node have. If a node has more edges than others, it has more “fans”, and gets more popular. Then, information provided by the popular node has a stronger ability to propagate than the “unknown” one. Meanwhile, the diffusion rate will attenuate with transmitting time growing.**



**it's the first work to establish a theoretical framework under which the impact of the shape of infection rate with consideration of the infected node's edges on the information diffusion dynamics is discussed!**



# Diffusion Models for Multi-Sensitive Networks

## Overview:

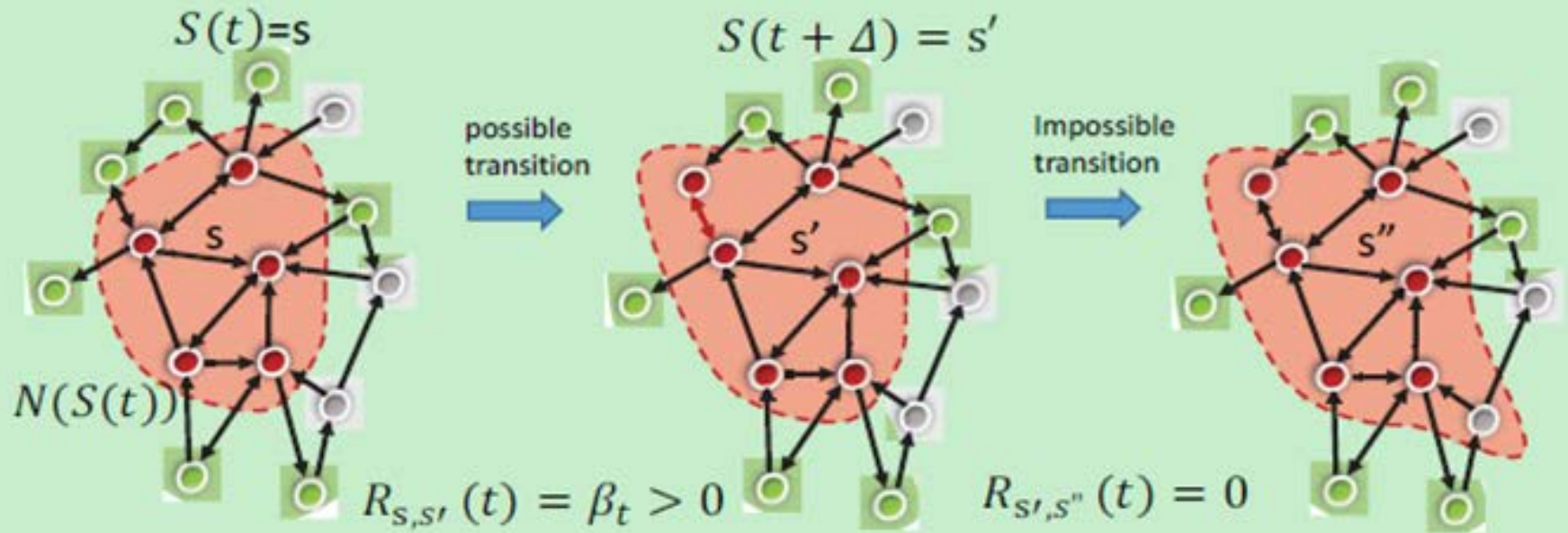
$$G = (N, E)$$

$$S(t) = (S_1(t), S_2(t), \dots, S_n(t)) \in \{0, 1\}^n$$

$$N(S(t)) = \{j \in N \setminus S(t) \mid \exists (i, j) \in E, i \in S(t)\}$$

$$\partial(S(t), j) = \{(i, j) \in E \mid i \in S(t), j \in N(S(t))\}$$

$$p_i = \beta \times |\partial(s(t, i))|$$







## Diffusion Models for Multi-Sensitive Networks

### Model of Time-sensitive information diffusion:

$$m(t) = \int_0^t \beta ds$$

$$\{S(t_1), S(t_2), \dots, S(t_r)\}$$

$$\{\check{S}(m(t_1)), \check{S}(m(t_2)), \dots, \check{S}(m(t_r))\}$$

$$p_i = \beta \times |\partial(s(t, i))| = \alpha \times t^\gamma \times |\partial(s(t, i))|$$



## Diffusion Models for Multi-Sensitive Networks

### Model of Edge-sensitive information diffusion:

For a homogeneous network

$$\beta = \alpha |\partial(s(t))|^\gamma$$

$$|\partial(s(t))| = \sum_{j \in N(S(t))} |\partial(S(t, j))|$$

$$E(V_t) = \alpha |\partial(s(t-1))|^{1+\gamma}$$



## Continue

$$E(|\partial(s(t-1))|) = m \times \frac{N - |s(t-1)|}{N-1} \times |s(t-1)|$$

$$s(t) = s(t-1) + V_t$$

$$E(V_t) = \alpha \left( m \times \frac{N - |s(t-1)|}{N-1} \times |s(t-1)| \right)^{1+\gamma}$$



**For an inhomogeneous network:**

$$p_i = \beta \times |\partial(s(t, i))|$$

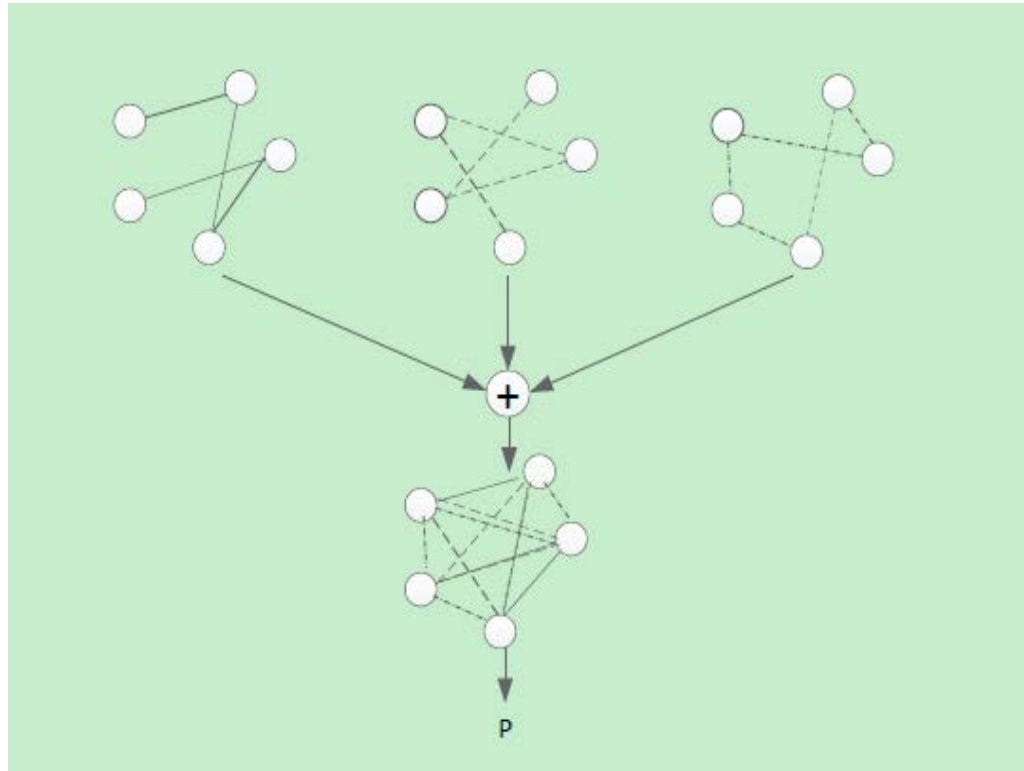
$$= \alpha \times \left[ \sum_{i \in R_t} \sum_{j \in \tau_t(i, k)} \delta(j, t) \right]^\gamma \times \sum_{j \in \tau_t(i, k)} \delta(j, t)$$

$$E(V_t) = \sum_{i \in R_t} p_i = \alpha \times \left[ \sum_{i \in R_t} \sum_{j \in \tau_t(i, k)} \delta(j, t) \right]^{\gamma+1}$$



## Model Information Diffusion in Multi-sensitive networks:

$$p_i = \sum_k \mu_k \times (\beta_i^{(k)} \times \sum_{j \in \tau_t(i,k)} \delta(j, t))$$





# Diffusion Model Learning From Action Log

## The Learning Framework:

$$P(V_t, R_t \setminus V_t) = \prod_{u \in V_t} p_u(t) \prod_{u \in R_t \setminus V_t} (1 - p_u(t))$$

$$L = \prod_k \prod_{t=1}^{T(k)} P(V_t^{(k)}, R_t \setminus V_t^{(k)})$$



## Diffusion Model Learning From Action Log

### Learning Algorithm:

$$\begin{aligned} \log(L) &= \sum_t \left\{ \sum_{u \in V_t} \log p_u(t) + \sum_{u \in V_t \setminus R_t} \log(1 - p_u(t)) \right\} \\ &= \sum_t \left\{ \sum_{u \in V_t} \log \sum_k \mu_k \beta_u^{(k)} \sum_{j \in \tau_t(u, k)} \delta(j, t) \right. \\ &\quad \left. + \sum_{u \in V_t \setminus R_t} \log \left[ 1 - \sum_k \mu_k \beta_u^{(k)} \sum_{j \in \tau_t(u, k)} \delta(j, t) \right] \right\} \end{aligned}$$



**Continue**

$$\mu_k^{new} = \mu_k^{old} + \eta \frac{\partial \log L}{\partial \mu_k}$$

**Action Prediction:**

$$E\left(\sum_{u \in R_t} Y_u(t)\right) = \sum_{u \in R_t} p_u(t)$$





## **Future Work**

- **find the theoretical proof of edge-sensitive model**
- **find the parameters that fits the time-edge-sensitive model best**
- **learning algorithms**